



South Central College

## MATH 130 Precalculus Mathematics

### Course Outcome Summary

#### Course Information

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| <b>Description</b>   | This is an accelerated course covering many topics from both College Algebra and Trigonometry. These include functions, graphs of functions, analytic geometry of the conic sections, systems of equations and inequalities, elementary matrix operations and determinants, properties and applications of exponential, logarithmic and trigonometric functions, complex numbers, vectors, polar coordinates and elementary combinatorics. Should not be taken for credit in addition to either MATH 120 or MATH 125. (Prerequisites: A score of 86 or higher on the College Level mathematics portion of the Accuplacer test.) (MNTC 4: Mathematical/Logical Reasoning) |
| <b>Total Credits</b> | 4  |
| <b>Total Hours</b>   | 64   |

#### Pre/Corequisites

A score of 86 or higher on the College Level mathematics portion of the Accuplacer test.

#### Institutional Core Competencies

Critical and Creative Thinking - Students will be able to demonstrate purposeful thinking with the goal of using a creative process for developing and building upon ideas and/or the goal of using a critical process for the analyzing and evaluating of ideas.

#### Course Competencies

##### 1. Graph elementary functions and relations accurately

###### Learning Objectives

- Graph linear functions
- Graph circles from their equations
- Deduce the equation of a circle from a given center and radius
- Compute vertex, axis of symmetry, increasing/decreasing behavior and intercepts of a parabola
- Calculate the domain and range of a quadratic function
- Graph more complex functions using transformations

##### 2. Describe functions in terms of the formal definition

###### Learning Objectives

- Define relations and functions precisely
- Apply the four binary arithmetic operators to functions
- Create composite functions

Prove a function is one-to-one  
Describe the relationship of a function to its inverse

### **3. Describe the local and global behavior of a given polynomial function**

#### **Learning Objectives**

Locate special points on the graphs of polynomial functions  
Graph polynomial functions using these special points  
Define what it means for a function to be an increasing or decreasing function on an interval

### **4. Compute the roots of polynomial equations**

#### **Learning Objectives**

Find rational zeroes using the Rational Root Theorem  
Predict polynomial behavior using Descartes' Rule of Signs  
Approximate real zeroes of polynomials

### **5. Evaluate expressions containing exponentials**

#### **Learning Objectives**

Define the general exponential function  
Find the domain and range of exponential functions  
Define the exponential function with base  $e$   
Graph exponential functions, along with any asymptotes  
Deduce laws of exponential growth and decay  
Model real-world problems using exponentials

### **6. Evaluate expressions containing logarithms**

#### **Learning Objectives**

Simplify logarithmic expressions using Napier's properties  
Define common and natural logarithms  
Change logarithmic expressions from one base to another  
Graph logarithmic functions

### **7. Solve equations containing exponentials and logarithms**

#### **Learning Objectives**

Specify behavior of such equations in terms of domain and range of the functions  
Solve certain exponential equations exactly  
Solve certain logarithmic equations exactly  
Approximate solutions to other exponential and logarithmic equations

### **8. Model real-world problems with radian measurements of angles**

#### **Learning Objectives**

Define the radian  
Convert between radian and degree measurements  
Apply radian measure to real-world problems

### **9. Define the six trigonometric functions as real valued functions of a real variable**

#### **Learning Objectives**

Explain the wrapping function and related circular functions  
Deduce domains and ranges for the six trigonometric functions  
Derive the Pythagorean and other simple properties of the trigonometric functions

### **10. Solve right triangle problems using trigonometry**

#### **Learning Objectives**

Model real-world problems using right triangles  
Solve for the missing parts in such problems using trigonometry

### **11. Graph trigonometric functions**

#### **Learning Objectives**

Check for symmetry among the six trigonometric functions

Locate any asymptotes  
Graph combination of trigonometric and algebraic functions using transformations

**12. Derive the six inverse trigonometric functions**

**Learning Objectives**

Find the domains and ranges of the inverse trigonometric functions  
Deduce other properties of the inverse trigonometric functions  
Graph the inverse trigonometric functions

**13. Derive useful results in analytic trigonometry**

**Learning Objectives**

Prove certain trigonometric identities  
Solve certain trigonometric conditional equations

**14. Compute the trigonometric functions of related angles**

**Learning Objectives**

Explain the trigonometric co-functions  
Compute the trigonometric functions of half-angles  
Compute the trigonometric functions of double-angles  
Find the trigonometric functions of a sum or difference of angles  
Convert trigonometric expressions of sums to products  
Convert trigonometric expressions of products to sums

**15. Apply trigonometry to oblique triangles**

**Learning Objectives**

Find the remaining parts of a triangle using the Law of Sines  
Find the remaining parts of a triangle using the Law of Cosines  
Apply (a) and (b), above, to real-world mensuration problems

**16. Interpret certain functions in polar coordinate form**

**Learning Objectives**

Transform functions from Cartesian to polar coordinate form  
Transform functions from polar coordinate to Cartesian form  
Deduce symmetry properties of functions expressed in polar coordinate form  
Graph functions expressed in polar coordinate form

**17. Express certain physical phenomena in terms of vectors**

**Learning Objectives**

Define geometric vectors  
Define algebraic vectors  
Establish properties of vectors and vector operations

**18. Perform operations on complex numbers**

**Learning Objectives**

Review complex number arithmetic  
Express complex numbers trigonometrically  
Graph complex numbers in the Cartesian and polar planes  
Use DeMoivre's Theorem to simplify powers of complex numbers

**19. Solve systems of linear equations using row operations or determinants**

**Learning Objectives**

Solve simple systems of linear equations using shorthand matrix concepts  
Solve systems of linear equations using Gauss-Jordan elimination  
Deduce basic properties of matrices and determinants  
Solve systems of linear equations with the Cramer's Rule

**20. Solve systems of linear inequalities**

**Learning Objectives**

Solve systems of linear inequalities in two variables  
Solve applied problems using elementary linear programming

**21. Predict the behavior of well-known sequences**

**Learning Objectives**

Generate individual terms from the definition of a sequence  
Create the most likely general term of a given finite sequence

**22. Define arithmetic sequences**

**Learning Objectives**

Generate individual terms in an arithmetic sequence  
Deduce the general term of an arithmetic sequence

**23. Define geometric sequences**

**Learning Objectives**

Generate individual terms in a geometric sequence  
Deduce the general term of a geometric sequence  
Apply geometric sequences to growth and decay problems

**24. Sum an arithmetic series**

**Learning Objectives**

Interpret the sigma sum notation  
Compute a sum knowing the first term, number of terms and the common difference  
Find the fourth item knowing any three items of part (b), above  
Visualize an arithmetic series geometrically  
Interpret the method of (d), above, in the context of what the ancient Greeks have given us

**25. Sum a geometric series**

**Learning Objectives**

Compute a sum knowing the first term, number of terms and the common ratio  
Sum an infinite geometric series when the ratio is appropriate

**26. Expand expressions using the Binomial formula**

**Learning Objectives**

Use Pascal's Triangle to rapidly compute coefficients  
Use the definition to compute the coefficients  
Find specific terms in a binomial expansion  
Expand a binomial raised to a power

**SCC Accessibility Statement**

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Additional information and forms can be found at: [www.southcentral.edu/disability](http://www.southcentral.edu/disability)

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